## Chapter 12: Estimating the Cost of Capital

Fundamental question: Where do we get the numbers to estimate the cost of capital?
$=>$ How do we implement the CAPM discussed in chapter 10 ?
12.1 The Equity Cost of Capital

Cost of capital: best expected return available in the market on investments with similar risk

$$
\begin{equation*}
r_{i}=r_{f}+\beta_{i} \times\left(E\left(R_{M k t}\right)-r_{f}\right) \tag{12.1}
\end{equation*}
$$

Notes:

1) We don't really need equation (12.1) since it is identical to equation (10.11)
2) Risk premium for security $i: \beta_{i} \times\left(E\left(R_{M k t}\right)-r_{f}\right)$

### 12.2 The Market Portfolio

A. Constructing the Market Portfolio

$$
\begin{equation*}
M V_{i}=N S O_{i} \times P_{i} \tag{12.2}
\end{equation*}
$$

where:
$M V_{i}=$ market value of $i$
$\mathrm{NSO}_{i}=$ number of shares of $i$ outstanding
$P_{i}=$ price of $i$ per share
$x_{i}=\frac{M V_{i}}{T M V}$
where:
$x_{i}=$ portfolio weight of security $i=\%$ of portfolio invested in security $i$ TMV = total market value of all securities in portfolio

Ex. Assume the market consists of five stocks: Alphabet, Ford, GE, Kellogg, and WalMart. The number of outstanding shares and current stock price for each firm are as follows:

| Name | Shares <br> (Billions) | Price |
| :--- | ---: | ---: |
| Alphabet | 0.4 | 650 |
| Ford | 4 | 15.05 |
| GE | 10 | 40 |
| Kellogg | 0.26 | 80 |
| Wal-Mart | 3.7 | 70 |

Assume also that you want to create a passive, value-weighted portfolio with $\$ 100,000$ that mimics market. How much do you need to invest in each company's shares? How many shares do you need to buy?

| Market |  |  |  |  | Portfolio |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Name | Shares <br> (Billions) | Price | Market Cap (Billions) | $x(i)$ | Investment | Shares | $x(i)$ | Percent of Shares |
| Alphabet | 0.4 | 650 | 260 | 0.26 | \$26,000.00 | 40 | 0.26 | 0.00001\% |
| Ford | 4 | 15.05 | 60.2 | 0.0602 | \$6,020.00 | 400 | 0.0602 | 0.00001\% |
| GE | 10 | 40 | 400 | 0.4 | \$40,000.00 | 1000 | 0.4 | 0.00001\% |
| Kellogg | 0.26 | 80 | 20.8 | 0.0208 | \$2,080.00 | 26 | 0.0208 | 0.00001\% |
| Wal-Mart | 3.7 | 70 | 259 | 0.259 | \$25,900.00 | 370 | 0.259 | 0.00001\% |
| Total |  |  | 1000 |  | \$100,000.00 |  |  |  |

Q: What changes do you need to make if the price per share of: Alphabet rises to $\$ 800$, Ford falls to $\$ 13$, GE falls to $\$ 30$, Kellogg rises to $\$ 95$, and Wal-Mart rises to $\$ 85$ ?

| Market |  |  |  |  | Portfolio |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Name | Shares <br> (Billions) | Price | Market Cap (Billions) | $x(i)$ | Investment | Shares | $x$ (i) for Portfolio | Percent of Shares |
| Alphabet | 0.4 | 800 | 320 | 0.32 | \$32,000.00 | 40 | 0.32 | 0.00001\% |
| Ford | 4 | 13 | 52 | 0.052 | \$5,200.00 | 400 | 0.052 | 0.00001\% |
| GE | 10 | 30 | 300 | 0.3 | \$30,000.00 | 1000 | 0.3 | 0.00001\% |
| Kellogg | 0.26 | 95 | 24.7 | 0.0247 | \$2,470.00 | 26 | 0.0247 | 0.00001\% |
| Wal-Mart | 3.7 | 85 | 314.5 | 0.3145 | \$31,450.00 | 370 | 0.3145 | 0.00001\% |
| Total |  |  | 1011.2 |  | \$101,120.00 |  |  |  |

Note: No need to rebalance value-weighted portfolio as stock prices change, but only if a firm issues or repurchases shares
Key: own same percent of each firm's outstanding shares as before the issue/repurchase ( $0.00001 \%$ in example).
B. Market Indexes

1. Examples of Market Indexes

Major U.S. stock indexes: S\&P 500 index, Nasdaq Composite Index (value-weighted index of more than 3000 common stocks listed on the Nasdaq stock exchange), and Dow Jones Industrial Average

Problems with DJIA: only 30 stocks, price- rather than value-weighted.
Notes:

1) we will use the $\mathbf{S \& P} 500$ as a proxy for the market
2) Dow Jones calculated by adding up prices and dividing by some number. Number started at 12 since there were 12 stocks, but equals 0.1517 as of the end of 2021 according to Investopedia.
2. Investing in a Market Index

Main ways to invest in a market index: index mutual funds, exchange-traded funds
Note: In my 403B (the non-profit equivalent to a 401k), I hold several Vanguard funds:

Total Stock Market Index (basically tracks the Wilshire 5000)
Value Index (tracks value stocks in the S\&P500), Total International Stock Index (tracks all non-US stocks) Small-Cap Value Index (tracks an index of small-cap value stocks) Short-Term Investment Grade (a short-term bond fund)

Reasons: I overweight value stocks because historically they have outperformed growth stocks with less risk. Based on my theoretical retirement date, I should hold some bonds, but I want to avoid long-term bonds since they will get hammered when interest rates eventually rise.

Value stock: slower growing firms with low PE ratios, high dividend yields, and low market to book ratios.
C. The Market Risk Premium

1. Determining the Risk-Free Rate

Notes:

1) We will use the yield on 10-year Treasuries as the risk-free rate.
2) Treasuries are subject to interest rate risk unless select a maturity equal to our investment horizon AND buy a U.S. Treasury Strip (pays no coupons).
$=>$ Otherwise, the coupons create interest rate risk as reinvest at an unknown rate.
2. The Historical Risk Premium
=> market risk premium over 10-year Treasuries:
$1926-2015=5.9 \%$
$1962-2015=3.9 \%$
Problems:
1) hard to know which past to use
2) difficult to have confidence in past since large standard errors
3) future may not be like the past
3. A Fundamental Approach

## Key $\Rightarrow>$ using current dividend yield and expected growth to estimate expected return on market

$$
\begin{equation*}
r_{M k t}=\frac{D_{1}}{P_{0}}+g \tag{12.4}
\end{equation*}
$$

Note: This is essentially equation (9.7), so we don't really need it.
Research: market risk premium estimated as being in $3-5 \%$ range.

### 12.3 Beta Estimation

## A. Using Historical Returns

=> beta depends on how sensitive firm's returns are to market returns
B. Identifying the Best-Fitting Line

## 1. beta equals slope of best-fitting line of excess returns on stock vs. excess returns on market

excess returns: return - risk-free rate
Ex. Assume you plot the excess monthly returns of Apple against the excess returns on the S\&P500 (see data at end of these notes) for 2017-2021.


Note: beta is approximately 1.21 based on the 5-years of monthly data
Note: Beta listed on Yahoo! Finance (as of $5 / 4 / 2022$ ) $=1.19$
2. deviations from line due to risk specific to the company
C. Using Linear Regression

$$
\begin{equation*}
\left(R_{i}-r_{f}\right)=\alpha_{i}+\beta_{i}\left(R_{M k t}-r_{f}\right)+\varepsilon_{i} \tag{12.5}
\end{equation*}
$$

where:
$\alpha_{i}=$ intercept term of regression
$\beta_{i}=$ beta of stock
$\mathcal{E}_{i}=$ error term $=$ risk unrelated to the market
$E\left[R_{i}\right]=r_{f}+\beta_{i}\left(E\left[R_{M k t}\right]-r_{f}\right)+\alpha_{i}$

Using Excel: Use the $\operatorname{SLOPE}()$ function to get $\beta$. Excess returns for the stock go in as the " $y$ " variable and excess returns for the market go in for the "x" variable. In the same way, you can use the INTERCEPT() function to get $\alpha$.

Note: If use $\operatorname{SLOPE}()$ function on excess return data at end of notes, also get beta of 1.21.
Ex. Calculate Apple's equity cost of capital if the risk-free rate equals $3 \%$ and the market risk premium equals $6 \%$.
$r_{e}=.1026=.03+\mathbf{1 . 2 1 ( . 0 6 )}$

### 12.4 The Debt Cost of Capital

Note: Both methods in this chapter give only an approximate debt cost of capital.

## A. Debt Yield Versus Returns

## Key: if chance of default, yield to maturity overstates the expected return on the bond

$r_{d}=(1-p) y+p(y-L)=y-p L$
where:
$y=$ yield to maturity on debt
$p=$ probability of default
$L=$ expected loss per dollar of debt if default
$r_{d}=$ debt cost of capital

Note: Table 12.2 is on the formula sheet

Table 12.2: Percent Annual Default Rates by Debt Rating

| Rating | AAA | AA | A | BBB | BB | B | CCC | CC-C |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Ave. | 0.0 | 0.1 | 0.2 | 0.5 | 2.2 | 5.5 | 12.2 | 14.1 |
| Recessions | 0.0 | 1.0 | 3.0 | 3.0 | 8.0 | 16.0 | 48.0 | 78.0 |

Ex. Assume that Kortly Inc. bond trade at a yield to maturity of $9 \%$. The bonds have a B rating and the expected loss in the event of default is $60 \%$. What is the expected return on Kortly debt?
$\mathrm{r}_{\mathrm{d}}=.057=.09-.055(.6)$
$=>$ once consider possible loss from default, expected return only equals $5.7 \%$.
B. Debt Betas
$=>$ difficult to calculate because of infrequent trading
$\Rightarrow$ will use data on average debt beta for bond rating and maturity Note: The betas by maturity are for bonds rated BBB or above.

Table 12.3: Average Debt Betas

| By Rating | A above | BBB | BB | B | CCC |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Avg. Beta | $<.05$ | .10 | .17 | .26 | .31 |
|  |  |  |  |  |  |
| By Maturity | $1-5 \mathrm{Yr}$ | $5-10 \mathrm{Yr}$ | $10-15 \mathrm{Yr}$ | $>15 \mathrm{Yr}$ |  |
| Avg. Beta | 0.01 | 0.06 | 0.07 | 0.14 |  |

Note: Table 12.3 is on the formula sheet
12.5 A Project's Cost of Capital

Key issue $=>$ can't directly estimate beta of project because not traded
=> use cost of capital from firms in same line of business as project
A. All-Equity Comparables

Optimal: firm in single line of business that is finance only with equity
=> use equity beta for comparables as beta for project
B. Levered Firms as Comparables

Key => return on assets equals return on portfolio of firm's debt and equity
C. The Unlevered Cost of Capital

$$
\begin{equation*}
r_{u}=\left(\frac{E}{E+D}\right) r_{e}+\left(\frac{D}{E+D}\right) r_{d} \tag{12.8}
\end{equation*}
$$

where:
$r_{u}=$ unlevered cost of capital $=$ expected return required by the firm's investors to hold the firm's underlying assets = weighted average of firm's equity and debt costs of capital
$E=$ total market value of equity
$D=$ total market value of debt
$r_{e}=$ equity cost of capital
$r_{d}=$ debt cost of capital
Ex. Assume Jaxter Inc. has $\$ 4$ million of outstanding debt and $\$ 10$ million of outstanding equity. Assume that the Jaxter's debt has a yield to maturity of $12 \%$. Assume also that you estimate that there is a $3 \%$ chance that Jaxter will default and that the loss in default will equal $40 \%$. Finally, assume that the equity cost of capital equals $16 \%$. Calculate Jaxter's unlevered cost of capital.

$$
\begin{aligned}
& \mathrm{r}_{\mathrm{d}}=.108=.12-.03(.4) \\
& r_{u}=.145=\left(\frac{10}{10+4}\right) \cdot 16+\left(\frac{4}{10+4}\right) \cdot 108=(.7143) \cdot 16+(.2857) \cdot 108
\end{aligned}
$$

1. Unlevered Beta

$$
\begin{equation*}
\beta_{u}=\left(\frac{E}{E+D}\right) \beta_{e}+\left(\frac{D}{E+D}\right) \beta_{d} \tag{12.9}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \beta_{u}=\text { unlevered beta } \\
& \beta_{e}=\text { equity beta } \\
& \beta_{d}=\operatorname{debt} \text { beta }
\end{aligned}
$$

Ex. Assume that Manstor Corp.'s equity has a beta of 1.1 and that its debt has a debt rating of BBB. Calculate Manstor's unlevered beta if it has $3,000,000$ outstanding shares that trade at a price of $\$ 30$ per share and has $\$ 25$ million of outstanding debt.

$$
\begin{aligned}
& \beta_{d}=\mathbf{0 . 1 0} \\
& \mathrm{E}=\$ 90 \text { million }=\mathbf{3 , 0 0 0 , 0 0 0} \times 30 \\
& \beta_{u}=0.883=.7826(1.1)+.2173(0.1)=\left(\frac{\mathbf{9 0}}{\mathbf{9 0 + 2 5}}\right) \mathbf{1} .1+\left(\frac{\mathbf{2 5}}{\mathbf{9 0 + 2 5}}\right) \mathbf{0 . 1}
\end{aligned}
$$

2. Cash and Net Debt

Key => want to estimate risk of underlying assets
=> cash is risk-free and reduces risk of firm
$=>$ estimate risk of firm's enterprise value (underlying business operations)
$=>$ can use net debt instead of debt when calculating unlevered cost of capital or unlevered beta

Note: The following is the same as equation (2.17).
$N D=D-E C$
where:

$$
N D=\text { net debt }
$$

$D=$ debt
$E C=$ excess cash and short-term investments
Note: often difficult to determine what portion of a firm's cash is "in excess of operating needs".

$$
\begin{equation*}
\beta_{E V}=\left(\frac{E}{E+D}\right) \beta_{e}+\left(\frac{D}{E+D}\right) \beta_{n d} \tag{12.A}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \beta_{E V}=\text { enterprise beta }=\text { beta of real assets } \\
& \beta_{e}=\text { equity beta } \\
& \beta_{n d}=\text { net debt beta }
\end{aligned}
$$

Ex. Assume a firm has $\$ 19$ million in real assets that have a beta of 1.2, but also has cash of $\$ 1$ million. Calculate the beta of the firm's assets. Note that cash free and so has a beta of 0 .

Key: The firm is a portfolio of real assets and cash so we can calculate the beta like any portfolio.

$$
\beta_{A}=\beta_{u}=1.14=(.95) 1.2+(.05) 0=\left(\frac{19}{19+1}\right) \mathbf{1 . 2}+\left(\frac{1}{19+1}\right) \mathbf{0}
$$

Ex. Assume we do not know the beta of the firm's real assets but do know the beta of the securities issued by the firm. The beta of the firm's equity is 1.425 and its debt is risk-free. The firm's equity is worth $\$ 16$ million and its debt is worth $\$ 4$ million. The firm has $\$ 1$ million of cash. Calculate the beta of the firm's operating assets

Net debt $=3=4-1$.

D. Industry Asset Betas
=> use average betas or average cost of capital for firms in same industry as project
=> reduces estimation error
12.6 Project Risk Characteristics and Financing
A. Differences in Project Risk

Key issues:

1) firm asset beta reflects risk of average asset in firm
2) identify "pure play" comparables for projects
3) adjust for differences in operating leverage by discounting fixed costs at risk-free risk-free or calculating beta of project's cash flows by recognizing fixed costs as having a zero beta.

See example 12.8
4) execution risk should be factored into estimates of cash flow
=> new investments by firm likely riskier than assets of established firms
$\Rightarrow>$ risk tends to be firm-specific and thus diversifiable
$\Rightarrow$ does not affect betas or cost of capital
=> does affect expected cash flows
B. Financing and the Weighted Average Cost of Capital
let:
$r_{a t}=$ effective after-tax interest rate
$r_{d}=$ pre-tax interest rate
$\tau_{c}=$ corporate tax rate

1. Perfect Capital Markets:
$\Rightarrow$ no taxes, transaction costs, or other frictions
$\Rightarrow$ all financing transactions are zero-NPV
$\Rightarrow$ use equation (12.8) on p. 9 (and shown again below).
$r_{U}=\left(\frac{E}{E+D}\right) r_{E}+\left(\frac{D}{E+D}\right) r_{d}$
2. Taxes - A Big Imperfection

Key issue $=>$ interest is tax deductible for companies

$$
\begin{equation*}
r_{a t}=r_{d}\left(1-\tau_{c}\right) \tag{12.11}
\end{equation*}
$$

Ex. Assume the yield to maturity on Lexing Inc's debt equals $8 \%$ and that there is a $10 \%$ chance that Lexing will default and the loss in case of default will equal $25 \%$. Calculate Lexing's effective after-tax interest rate if the corporate tax rate equals $21 \%$.

$$
\begin{aligned}
& r_{d}=.055=.08 \mathbf{- . 1 ( . 2 5 )} \\
& r_{a t}=.04345=. \mathbf{0 5 5 ( 1 - . 2 1 )}
\end{aligned}
$$

Note: Equation (12.11) is the same as equation (5.8)
3. The Weighted Average Cost of Capital

$$
\begin{equation*}
r_{w a c c}=\left(\frac{E}{E+D}\right) r_{E}+\left(\frac{D}{E+D}\right) r_{d}\left(1-\tau_{c}\right) \tag{12.12}
\end{equation*}
$$

Notes:

1) incorporates tax shield from debt financing into NPV
2) can use $r_{u}$ to evaluate all-equity financed projects and $r_{\text {wacc }}$ to evaluate projects with same financing as the firm.
3 ) corporate taxes are not the only market imperfection related to financing choices
$r_{w a c c}=r_{u}-\left(\frac{D}{E+D}\right) \tau_{c} r_{d}$
=> WACC equals unlevered cost of capital less tax savings of debt
$\Rightarrow$ lower cost of capital increases NPV

Ex. Assume that Waldy has 100,000 outstanding shares and that these shares have a market value of $\$ 40$ per share. Assume also that Waldy has $\$ 500,000$ of outstanding debt that is risk free. Assume that the risk-free rate equals $4 \%$ and that the expected return on the market equals $9 \%$. If Waldy's stock has a beta of 1.3 and the corporate tax rate equals $21 \%$, calculate Waldy's weighted average cost of capital?
$\mathrm{E}=4,000,000=\mathbf{1 0 0 , 0 0 0} \mathbf{x} \mathbf{4 0}$
$r_{e}=.105=.04+1.3(.09-.04)$
$r_{\text {wacc }}=.0968=\left(\frac{4,000,000}{4,000,000+500,000}\right) \cdot 105+\left(\frac{500,000}{4,000,000+500,000}\right) \cdot \mathbf{0 4}(\mathbf{1}-.21)$ $=(.889) \cdot 105+(.111) \cdot 0316$
or:
$r_{u}=.09778=\left(\frac{4,000,000}{4,000,000+500,000}\right) \cdot 105+\left(\frac{\mathbf{5 0 0}, 000}{4,000, \mathbf{0 0 0}+\mathbf{5 0 0}, \mathbf{0 0 0}}\right) \cdot \mathbf{0 4}$
$r_{\text {wacc }}=.0968=.09778-\left(\frac{500,000}{4,000,000+500,000}\right) \times .21 \times .04$
12.7 Final Thoughts on Using the CAPM

1) CAPM based on estimates, but so are cash flows
2) errors in model tend to be smaller than if use other models
3) using CAPM forces managers to think about cost of capital
4) using CAPM forces managers to think about risk in correct way

Appendix: Practical Considerations When Forecasting Beta
A. Time Horizon
=> too short a horizon: unreliable estimates
$=>$ too long a horizon: older data no longer reflects firm's current risk
B. The Market Proxy
$=>$ S\&P 500 is usual proxy, but others are used
=> especially when evaluating international investments
$\Rightarrow$ match market risk premium with market proxy used
C. Beta Variation and Extrapolation
$=>$ betas tend to regress towards 1.0 over time
$=>$ adjusted betas take weighted average of computed beta and 1 .
D. Outliers
=> beta estimates sensitive to outliers (especially large or small returns)
Comment: knowing which returns to exclude as outliers is tricky. Notice in Figure 12A. 2 that Genentech had other returns that were higher and lower than those excluded.
E. Other considerations
$=>$ be aware of changes in firm
$=>$ forecasting is more art than science
Comment: this is generally true for finance as a whole

Data Appendix: Price Data for Apple and S\&P500 and Yield on 10-year Treasuries

|  | Prices |  | Yield |  | Returns |  | Excess Returns |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Date | S\&P500 | Apple | 10yTr | 10y(mo) | S\&P500 | Apple | S\&P500 | Apple |
| 12/31/2021 | 473.49 | 177.34 | 1.512 | 0.0013 | 0.0462 | 0.0742 | 0.0450 | 0.0730 |
| 11/30/2021 | 452.56 | 165.09 | 1.443 | 0.0012 | -0.0080 | 0.1051 | -0.0092 | 0.1039 |
| 10/31/2021 | 456.22 | 149.39 | 1.557 | 0.0013 | 0.0702 | 0.0587 | 0.0689 | 0.0574 |
| 9/30/2021 | 426.31 | 141.11 | 1.529 | 0.0013 | -0.0466 | -0.0680 | -0.0479 | -0.069 |
| 8/31/2021 | 447.15 | 151.42 | 1.304 | 0.0011 | 0.0298 | 0.0425 | 0.0287 | 0.04 |
| 7/31/2021 | 434.23 | 145.24 | 1.239 | 0.0010 | 0.0244 | 0.0650 | 0.0234 | 0.0640 |
| 6/30/2021 | 423.88 | 136.38 | 1.443 | 0.0012 | 0.0224 | 0.0991 | 0.0212 | 0.0979 |
| 5/31/2021 | 414.58 | 124.0 | 1.581 | 0.0013 | 0.0066 | -0.0505 | 0.0053 | -0.0518 |
| 4/30/2021 | 411.88 | 130.68 | 1.631 | 0.0013 | 0.0529 | 0.0762 | 0.0516 | 0.0749 |
| 3/31/2021 | 391.18 | 121.43 | 1.746 | 0.0014 | 0.0454 | 0.0073 | 0.0440 | 0.005 |
| 2/28/2021 | 374.19 | 120.54 | 1.46 | 0.0012 | 0.0278 | -0.0797 | 0.0266 | -0.080 |
| 1/31/2021 | 364.07 | 130.98 | 1.093 | 0.0009 | -0.0102 | -0.0055 | -0.0111 | -0.0064 |
| 12/31/2020 | 367.8 | 131.71 | 0.917 | 0.0008 | 0.0370 | 0.1146 | 0.0363 | 0.11 |
| 11/30/2020 | 354.68 | 118.17 | 0.844 | 0.0007 | 0.1088 | 0.0955 | 0.1081 | 0.0948 |
| 10/31/2020 | 319.88 | 107.87 | 0.86 | 0.0007 | -0.0249 | -0.0600 | -0.0256 | -0.0607 |
| 9/30/2020 | 328.06 | 114.76 | 0.677 | 0.0006 | -0.0374 | -0.1025 | -0.0380 | -0.1031 |
| 8/31/2020 | 340.82 | 127.87 | 0.693 | 0.0006 | 0.0698 | 0.2166 | 0.0692 | 0.2160 |
| 7/31/2020 | 318.59 | 105.10 | 0.536 | 0.0004 | 0.0589 | 0.1651 | 0.0584 | 0.1647 |
| 6/30/2020 | 300.87 | 90.21 | 0.653 | 0.0005 | 0.0177 | 0.1474 | 0.0172 | 0.1 |
| 5/31/2020 | 295.63 | 78.62 | 0.648 | 0.0005 | 0.0476 | 0.0851 | 0.0471 | 0.08 |
| 4/30/2020 | 282.18 | 72.45 | 0.622 | 0.0005 | 0.1270 | 0.1554 | 0.1265 | 0.1549 |
| 3/31/2020 | 250.39 | 62.71 | 0.698 | 0.0006 | -0.1249 | -0.0698 | -0.1255 | -0.0703 |
| 2/29/2020 | 286.11 | 67.41 | 1.127 | 0.0009 | -0.0792 | -0.1147 | -0.0801 | -0.115 |
| 1/31/2020 | 310.71 | 76.15 | 1.52 | 0.0013 | -0.0004 | 0.0540 | -0.0017 | 0.0528 |
| 12/31/2019 | 310.84 | 72.25 | 1.919 | 0.0016 | 0.0291 | 0.0988 | 0.0275 | 0.09 |
| 11/30/2019 | 302.06 | 65.75 | 1.776 | 0.0015 | 0.0362 | 0.0776 | 0.0347 | 0.07 |
| 10/31/2019 | 291.51 | 61.02 | 1.691 | 0.0014 | 0.0221 | 0.1107 | 0.0207 | 0.109 |
| 9/30/2019 | 285.20 | 54.94 | 1.675 | 0.0014 | 0.0195 | 0.0730 | 0.0181 | 0.0716 |
| 8/31/2019 | 279.76 | 51.20 | 1.506 | 0.0012 | -0.0167 | -0.0165 | -0.0180 | -0.0177 |
| 7/31/2019 | 284.52 | 52.06 | 2.021 | 0.0017 | 0.0151 | 0.0764 | 0.0135 | 0.0747 |
| 6/30/2019 | 280.29 | 48.36 | 2 | 0.0017 | 0.0696 | 0.1305 | 0.0679 | 0.1289 |
| 5/31/2019 | 262.05 | 42.78 | 2.142 | 0.0018 | -0.0638 | -0.1242 | -0.0655 | -0.1260 |
| 4/30/2019 | 279.90 | 48.85 | 2.509 | 0.0021 | 0.0409 | 0.0564 | . 0388 | 0.0544 |
| 3/31/2019 | 268.92 | 46.24 | 2.414 | 0.0020 | 0.0181 | 0.0970 | 0.0161 | 0.09 |
| 2/28/2019 | 264.13 | 42.15 | 2.711 | 0.0022 | 0.0324 | 0.0448 | 0.0302 | 0.04 |
| 1/31/2019 | 255.84 | 40.34 | 2.635 | 0.0022 | 0.0801 | 0.0552 | 0.0779 | 0.05 |
| 12/31/2018 | 236.88 | 38.23 | 2.686 | 0.0022 | -0.0880 | -0.1167 | -0.0903 | -0.1189 |
| 11/30/2018 | 259.75 | 43.29 | 3.013 | 0.0025 | 0.0185 | -0.1812 | 0.016 | -0.1837 |
| 10/31/2018 | 255.02 | 52.86 | 3.159 | 0.0026 | -0.0691 | -0.0305 | -0.071 | -0.03 |
| 9/30/2018 | 273.95 | 54.53 | 3.056 | 0.0025 | 0.0059 | -0.0083 | 0.0034 | -0.01 |
| 8/31/2018 | 272.33 | 54.98 | 2.853 | 0.0023 | 0.0319 | 0.2004 | 0.0296 | 0.198 |
| 7/31/2018 | 263.90 | 45.80 | 2.964 | 0.0024 | 0.0370 | 0.0280 | 0.0346 | 0.0255 |
| 6/30/2018 | 254.48 | 44.56 | 2.849 | 0.0023 | 0.0058 | -0.0094 | . 0034 | -0.0118 |
| 5/31/2018 | 253.02 | 44.98 | 2.822 | 0.0023 | 0.0243 | 0.1351 | 0.0220 | 0.1328 |
| 4/30/2018 | 247.02 | 39.63 | 2.936 | 0.0024 | 0.0052 | -0.0150 | 0.0028 | -0.01 |
| 3/31/2018 | 245.75 | 40.23 | 2.741 | 0.0023 | -0.0274 | -0.0581 | -0.0297 | -0.0603 |
| 2/28/2018 | 252.67 | 42.71 | 2.868 | 0.0024 | -0.0364 | 0.0682 | -0.0387 | 0.0658 |
| 1/31/2018 | 262.21 | 39.98 | 2.72 | 0.0022 | 0.0564 | -0.0106 | 0.0541 | -0.0129 |
| 12/31/2017 | 248.22 | 40.41 | 2.405 | 0.0020 | 0.0121 | -0.0152 | 0.0101 | -0.0172 |
| 11/30/2017 | 245.24 | 41.04 | 2.417 | 0.0020 | 0.0306 | 0.0203 | 0.0286 | 0.0183 |
| 10/31/2017 | 237.97 | 40.22 | 2.376 | 0.0020 | 0.0236 | 0.0968 | 0.0216 | 0.0948 |
| 9/30/2017 | 232.49 | 36.67 | 2.326 | 0.0019 | 0.0201 | -0.0602 | 0.0182 | -0.0622 |
| 8/31/2017 | 227.90 | 39.02 | 2.121 | 0.0018 | 0.0029 | 0.1070 | 0.0012 | 0.1052 |
| 7/31/2017 | 227.24 | 35.25 | 2.292 | 0.0019 | 0.0206 | 0.0327 | 0.0187 | 0.0308 |
| 6/30/2017 | 222.66 | 34.13 | 2.302 | 0.0019 | 0.0064 | -0.0572 | 0.0045 | -0.059 |
| 5/31/2017 | 221.25 | 36.21 | 2.196 | 0.0018 | 0.0141 | 0.0678 | 0.0123 | 0.0660 |
| 4/30/2017 | 218.17 | 33.91 | 2.282 | 0.0019 | 0.0099 | -0.0001 | 0.0080 | -0.0020 |
| 3/31/2017 | 216.03 | 33.91 | 2.396 | 0.0020 | 0.0012 | 0.0487 | -0.0007 | 0.0467 |
| 2/28/2017 | 215.76 | 32.34 | 2.358 | 0.0019 | 0.0393 | 0.1338 | 0.0373 | 0.1318 |
| 1/31/2017 | 207.60 | 28.52 | 2.451 | 0.0020 | 0.0179 | 0.0477 | 0.0159 | 0.0457 |
| 12/31/2016 | 203.95 | 27.22 | 2.446 | 0.0020 |  |  |  |  |

## Notes:

1) Last Trade $=$ last trading day of each month. Prices are Yahoo's Adjusted Close which adjusts for dividends
2) $10 y(\mathrm{mo})=$ return per month on 10 -year Treasuries (to match monthly stock returns)
3) Returns $=($ price $($ current $)-$ price $($ prior $)) /$ price $($ prior $)$
4) Excess returns $=$ returns $-10 y(\mathrm{mo})$
