Chapter 6 - Example 3

Assume a corporate bond with a $\$ 1000$ face value matures 5 years and 7 months from today and has an annual coupon rate of $8 \%$ paid semiannually. There is a $10 \%$ chance that the issuer will default at maturity. If the firm defaults, it will pay $80 \%$ of what is promised (final coupon + face value) at maturity. But it will pay all coupons prior to maturity even if it defaults at maturity. Treasuries with the same maturity earn a yield to maturity of $2 \%$ and investors in these corporate bonds demand a $3 \%$ risk premium over the current rate on Treasuries (thus requiring an expected return of 5\%) to compensate for the risk they face (All rates are APR with semiannual compounding).

Calculate the clean price of the bond.


$$
\begin{aligned}
& y=\frac{.05}{2}=.025 \\
& E(T)=.9 \times 1045+.1 \times .8 \times 1040=1019.20
\end{aligned}
$$

$$
V_{-5 n}=\left(\frac{40}{(0.05}\right)\left(1-\left(\frac{1}{1.055}\right)^{11}+\frac{E(T)}{(1.055)^{12}}=380.57+757.83=1138.40\right.
$$

$$
\begin{aligned}
& V_{0}=1138.40(1.075)^{5 / 6}=1162.07 \\
& \text { clean }=1162.07-\left(\frac{5}{6}\right)(40)=1128.73
\end{aligned}
$$

