## Chapter 3: Financial Decision Making and the Law of One Price

Fundamental question: What are assets worth?
$=>$ starting point: any two assets that always pay the same cash flows should have the same price
$=>$ if not the case, whoever notices it can make a lot of money very quickly.
$=>$ all mispriced assets will disappear almost immediately as bought (if price too low) or sold (if price too high)
3.1 Valuing Decisions

Key issues:
=> good decision: benefits exceed costs
$\Rightarrow$ role of other disciplines in financial decisions: marketing, accounting, economics, organizational behavior, strategy, operations
A. Analyzing Costs and Benefits

Key issues:
$=>$ quantify costs and benefits
=> equivalent cash today
B. Using Market Prices to Determine Cash Values
a. Definitions and example
b. Competitive market: goods can be bought and sold at the same price

Q: Do such markets exist?
=> The NYSE is pretty close
Bid price: highest price at which anyone is willing to buy
Ask price: lowest price at which anyone is willing to sell
=> see price data on Ford
Notes:

1) anyone can submit their own bid or ask price
=> called a limit order
2) anyone submitting a market order takes whatever price exists in the market now
=> if buying, they'll pay the ask price (the lowest price that anyone is willing to sell for)
$=>$ if selling, they'll get the bid price (the highest price that anyone is willing to pay).
b. Equivalent value today if competitive market: market price

Note: value doesn't depend on individual preferences or expectations
Ex. Assume your uncle gives your 100 shares of Ford. What is the gift worth?
Ex. Would you trade your shares for $\$ 1000$ ?
Ex. Would you trade your shares for 100 shares of Honda?
2. When a competitive market does not exist

Note: This is when finance gets more interesting
Ex. Ford dealership on Hwy 84 in Waco (Bird Kultgen)
a. Equivalent value today: present value of future cash flows

Notes:

1) cash flows at different points in time are in different units $=>$ can't combine or compare them
2) interest rate: exchange rate across time $\Rightarrow$ allows us to convert dollar at one point in time to another point in time
3) interpretation: present value $=$ amount would need to invest today at the current interest rate to end up with the same cash flow in the future
3.2 Interest rates and the Time Value of Money

Key issues:
$=>$ think of borrowing and lending to convert money between future and today
$=>$ will start with known cash flows and a risk-free interest rate
Comment: Discussing the time value of money in terms of exchange rates (as the textbook does) is excellent. Another slightly different way to think about the time value of money follows. Think about the issue whichever way makes the most sense to you.
A. Future values

Note: the future value of any amount paid or received today equals the cash have
today plus interest would earn over the coming year if had invested it
Ex. How much will you have one year from today if you invest \$100 today at an interest rate of $1 \%$ per year? (What is the future value of $\$ 100$ ?)

Interest = \$1 = $\mathbf{1 0 0} \mathbf{x} . \mathbf{0 1}$
Amount have in one year $=\$ 101=\mathbf{1 0 0}+\mathbf{1}$
General Equation:
Let:
$C_{t}=$ cash " t " years from today
Notes:

1) cash inflows are positive and cash outflows are negative
2) $C_{0}=$ cash today
3) $C_{1}=$ cash a year from today
$I_{t}=$ interest earned over year $t$
Note: $I_{l}=$ interest earned between today and a year from today
$r=$ interest rate
$V_{t}=$ value " t " years from today
Notes:
4) $V_{0}=$ value today
5) $P V=$ present value $=V_{0}$
6) $V_{l}=$ value a year from today
$V_{1}=C_{0}+I_{1}=C_{0}+C_{0} \times r=C_{0}(1+r)$
$V_{1}=C_{0}(1+r)$
Ex.

$$
V_{1}=100(1.01)=\$ 101
$$

B. Present values
$=>$ the present value of any cash paid or received in the future equals the amount of future cash the less interest could have earned if had invested the present value today.

Ex. How much must you deposit today to have $\$ 101$ a year from today if the interest rate is $1 \%$ ? (What is the present value of $\$ 101$ ?)

Note: From previous example, we know the answer has to be $\$ 100$ !

$$
\begin{aligned}
\mathrm{PV} & =\mathrm{V}_{0}=101-\mathrm{I}_{1} \\
& \Rightarrow \mathrm{~V}_{0}=101-\mathrm{V}_{0}(.01) \\
& \Rightarrow \mathrm{V}_{0}+\mathrm{V}_{0}(.01)=101 \\
& \Rightarrow \mathrm{~V}_{0}(1.01)=101 \\
& \Rightarrow V_{0}=\frac{101}{1.01}=100
\end{aligned}
$$

General Equation:

$$
\begin{align*}
V_{0} & =C-I=C_{1}-r \times V_{0} \\
& =>V_{0}+r \times V_{0}=C_{1} \\
& =>V_{0}(1+r)=C_{1} \\
V_{0} & =\frac{C_{1}}{(1+r)} \tag{3.B}
\end{align*}
$$

Ex.

$$
V_{0}=\frac{C_{1}}{(1+r)}=\frac{\mathbf{1 0 1}}{(\mathbf{1 . 0 1})}=\mathbf{1 0 0}
$$

3.3 Present Value and the NPV Decision Rule

1) $\mathrm{NPV}=$ present value of all cash flows (inflows and outflows)
2) Interpretation of NPV: wealth created by project
3) Accept all positive NPV projects or the highest NPV project if must chose
4) Another way to think about it: NPV equals the difference between the cost of the project and how much it would cost to recreate a project's cash flows at the current interest rate
5) Decision doesn't depend on preference for cash today vs. cash in the future

Ex. Assume you have an opportunity to buy land for $\$ 110,000$ that you will be able to sell for $\$ 120,000$ a year from today. Further assume that all cash flows are known for sure and that you can borrow or lend at a risk-free interest rate of $4 \%$.
a. Should you buy the land if you have $\$ 110,000$ ?

$$
N P V=-110,000+\frac{120,000}{1.04}=-110,000+115,384.60=5384.6
$$

Q: How much would you have to invest at $4 \%$ to end up with $\$ 120,000$ a year from
today?
=> \$115,384.60
Q: How much better off are you if you buy the land? \$5384.60
b. Should you buy the land if you have no money?
$=>$ yes
Q: How?
$=>$ borrow $\$ 115,384.60$ and buy the land for $\mathbf{\$ 1 1 0 , 0 0 0}$
$=>$ keep $\$ 5384.60$ today
$=>$ in one year sell the land and use the proceeds to pay off the loan
Q : Is it realistic to assume that a firm or individual could borrow more than a project costs and to keep the difference?

A: Not really. Rules implemented after the global financial crisis of 2007-2008 prevent borrowing more than the value of an asset. Before the financial crisis, some people borrowed more than the value of a house, but most of that involved fraud. But the idea is theoretically sound.
3.4 Arbitrage and the Law of One Price
A. Key issues:
=> equivalent assets: assets with exactly the same cash flows in all periods under all conditions
$\Rightarrow$ arbitrage: trading to take advantage of price differences between equivalent assets possibly trading in different markets
=> key: buy low-priced asset and simultaneously sell the high-priced-asset
Notes:

1) requires no investment and creates riskless payoff today
2) as arbitrage occurs, all mispriced assets get bought and sold very quickly

Ex. Assume GE trades for $\$ 14$ on the New York Stock Exchange and for $\$ 13$ on the CBOE exchange
=> arbitrage: simultaneously buy GE on CBOE and sell it on NYSE

$$
\Rightarrow \text { trade as many sets of shares (buy and sell) as possible }
$$

Ex. Assume the following prices for HMC stock are available on the CBOE and the New York Stock exchange:

Note: HMC stock traded on CBOE and NYSE are equivalent since same exact asset

HMC
CBOE

| Bid |  | Ask |  |
| ---: | ---: | ---: | ---: |
| $\frac{\text { Price }}{32.73}$ | $\frac{\text { Shares }}{400}$ | $\frac{\text { Price }}{32.76}$ | $\frac{\text { Shares }}{300}$ |

Q: What transactions create arbitrage? What is the profit?
Arbitrage: simultaneously buy shares on the CBOE and sell shares on the NYSE for risk-free profit of $\mathbf{\$ 7 2 0}$.

Note: Arbitrage profit $=\mathbf{6 0 0 0} \times \mathbf{( 2 5 . 8 8} \mathbf{- 2 5 . 7 6})$
Q: Why do we use $\$ 25.88$ and $\$ 25.76$ ?
Q: Why not trade more than 6000 shares?
Q: How long will these conditions last?
=> exploiting arbitrage eliminates arbitrage opportunities
$=>$ law of one price: equivalent assets trading in different competitive markets must have same price in both markets
=> normal market: competitive market in which there are no arbitrage opportunities
B. Short-selling

Note: There is no problem if arbitrage requires selling an asset you don't own
=> short-sell the asset

1) today: borrow a security (usually from a broker) and sell it
2) later: buy same security and give it back to whoever you borrowed it from

Notes:

1) if the security has matured, might pay the cash value rather than buying the security and giving it back
2) must make up any cash flows the lender would have received while the security was borrowed
3) short seller can buy and return the security at any time
4) lender can demand the return of the loaned security at any time

Ex. Assume you want to short-sell 100 shares of GE today for the market price of $\$ 12.50$ per share

1) borrow 100 shares from your broker and sell them on the NYSE

Q: Where stand?
=> owe your broker 100 shares of GE
$\Rightarrow$ have $\$ 1250$ in your brokerage account
2) assume price falls from $\$ 12.50$ to $\$ 10$
3) Q: How close out short position?
$=>$ buy 100 shares at $\mathbf{\$ 1 0}$ per share and give the shares to your broker
4) assume that while you were short GE paid a dividend of $\$ 0.15$ per share $=>$ must give $\$ 15$ to your broker.
5) Profit $=+235=+\mathbf{1 2 5 0}-\mathbf{1 5}-\mathbf{1 0 0 0}$
3.5 No-Arbitrage and Security Prices
A. Valuing a security with the law of one price

Key: For there to be no arbitrage, the price of any security must equal the present value of its cash flows

Ex. Assume you can borrow or lend at the risk-free rate of $7 \%$ and that a risk-free bond pays $\$ 1000$ a year from today
$P V=\frac{1000}{1.07}=934.58$
a) Assume price of bond is $\$ 920$ (rather than its present value) $=>$ arbitrage is possible

Goal in arbitrage: positive cash flow today, no possible net cash flow after today
Basic questions to ask when setting up an arbitrage:

1) What transaction (or set of transactions) is equivalent to the security?
2) Do you want to buy or sell the security?
3) What cash flows does this create?
4) What transaction today offsets the security's cash flows in the future and
creates a profit today?
Q: What are equivalent transactions?

| Equivalent Transaction | $\frac{\text { Transaction }}{\text { Equivalent to buying bond }}$ | $\frac{\text { Sin one year }}{\text { Lend } \$ 934.58}$ |
| :--- | :--- | :---: |
| Equivalent to short-selling bond | Borrow $\mathbf{\$ 9 3 4 . 5 8}$ | $\mathbf{- \$ 1 0 0 0}$ |

Q: Buy or sell the bond if the price is $\$ 920$ rather than $\$ 934.58$ ?
Q: What are cash flows if trade the bond?
Q: How end up with no cash flow next year?

| Transaction( $\mathrm{t}=0$ ) | \$ today | \$ in one year | $\underline{\text { Transaction( } \mathrm{t}=1)}$ |
| :---: | :---: | :---: | :---: |
| Buy bond | -920.00 | +1000.00 | Payoff from bond |
| Borrow \$934.58 | +934.58 | $\underline{\mathbf{- 1 0 0 0 . 0 0}}$ | Pay off loan |
| Total | +14.58 | 0.00 |  |

Arbitrage profit $=\mathbf{\$ 1 4 . 5 8}$
b) Assume price of bond is $\$ 950$ rather than $\$ 934.58$

Q: Buy or sell the bond?
Q: What are cash flows if trade the bond?
Q: How end up with no cash flow next year?

| Transaction ( $\mathrm{t}=0$ ) | \$ today | \$ in one year | Transaction ( $\mathrm{t}=1$ ) |
| :---: | :---: | :---: | :---: |
| Short-sell bond | +950.00 | -1000.00 | Buy back bond, give to lender |
| Lend \$934.58 | -934.58 | $\underline{+1000.00}$ | Payoff on loan |
| Total | +15.42 | 0.00 |  |

Arbitrage profit $=\mathbf{\$ 1 5 . 4 2}$
$=>$ only way there is no arbitrage: price $=\mathbf{\$ 9 3 4 . 5 8}$
Notes:

1) investors rushing to take advantage of the arbitrage opportunity will quickly drive the price to $\$ 934.58$
2) interest rates are usually extracted from security prices rather than the other way around

Ex. What is usually known: $\mathrm{CF}_{1}=\$ 1000$, Price $=\$ 934.58$

$$
\Rightarrow 934.58=\frac{1000}{1+r}=>\mathrm{r}=.07=7 \%
$$

B. In a normal market, buying and selling securities has zero NPV

Keys:
a) $\operatorname{NPV}($ buying security $)=\mathbf{P V}(\mathbf{C F})$ - price
$\Rightarrow$ in normal market, price $=P V(C F)$
b) $\operatorname{NPV}($ selling security $)=$ price $-\mathbf{P V}(\mathbf{C F})$
$\Rightarrow$ in normal market, price $=P V(C F)$
=> otherwise arbitrage possible
C. Valuing a Portfolio

Portfolio: collection of securities
Key: In a normal market, equivalent portfolios (exactly same cash flows) must have same price
=> otherwise arbitrage is possible

1. ETF: exchange traded fund
$=>$ essentially a portfolio of securities that you can trade on an exchange
2. Value Additivity: the price of a portfolio must equal the combined values of the securities in the portfolio

$$
\begin{equation*}
\Rightarrow \operatorname{Price}(\mathrm{A}+\mathrm{B})=\operatorname{Price}(\mathrm{A})+\operatorname{Price}(\mathrm{B}) \tag{3.5}
\end{equation*}
$$

Ex. Assume the following:
ETF1 has one share of security A and one share of security B.
ETF2 has one share of security $C$ and one share of security D.
Security A pays $\$ 100$ a year from today and has a market price of \$95.24.
Security B pays $\$ 150$ a year from today and has a market price of $\$ 142.86$.
Security C pays $\$ 200$ a year from today and Security D pays $\$ 50$ a year from today.
Q: What portfolio is equivalent to ETF1?
$\frac{\text { Transaction }}{\text { Buy ETF1 }} \frac{\text { \$in one year }}{+250.00}$

Equivalent portfolio:
Buy A $\quad+100.00$
Buy B $\quad+\underline{150.00}$

Total +250.00
$=>$ buying a share of $A$ and a share of $B$ is equivalent to buying the ETF
Q: What is the no-arbitrage price be for ETF1?
$=>\mathbf{2 3 8 . 1 0}=\mathbf{9 5 . 2 4}+\mathbf{1 4 2 . 8 6}$
Reason: ETF1 must have the same price as a portfolio of A and B
Key to arbitrage with equivalent portfolios with different prices: buy low and sell high

Assume price of ETF1 is $\$ 220$ instead of $\$ 238.10$
Arbitrage: Buy ETF1, short-sell equivalent portfolio

| Transaction ( $\mathrm{t}=0$ ) | \$ today | \$ in one year | $\underline{\text { Transaction (t=1) }}$ |
| :---: | :---: | :---: | :---: |
| Buy ETF1 | -220.00 | +250.00 | Payoff on ETF |
| Short-sell A | +95.24 | -100.00 | Buy back A, return to lender |
| Short-sell B | +142.86 | $\underline{\mathbf{- 1 5 0 . 0 0}}$ | Buy back B, return to lender |
| Total | +18.10 | 0.00 |  |

Assume price of ETF1 is $\$ 245$ instead of $\$ 238.10$
Arbitrage: short-sell ETF1, buy equivalent portfolio

| Transaction ( $\mathrm{t}=0$ ) | \$ today | \$ in one year | Transaction ( $\mathrm{t}=1$ ) |
| :---: | :---: | :---: | :---: |
| Short-sell ETF1 | +245.00 | -250.00 | Buy back ETF, return to lender |
| Buy A | -95.24 | +100.00 | Payoff on A |
| Buy B | $\underline{-142.86}$ | +150.00 | Payoff on B |
| Total | +6.90 | 0.00 |  |

$\Rightarrow$ only way no arbitrage: price of ETF1 $=238.10$
$=>$ arbitrage will quickly drive the price of ETF1 to $\$ 238.10$
Q: What does the market price for ETF2 have to be?
Note: payoff on ETF2 next year: $200+50=250$
Q: What portfolio is equivalent to ETF2?
=> ETF1
=> must be worth 238.10
Reason: otherwise arbitrage is possible between ETF1 and ETF2
2. Value Additivity and Firm Value

Key issues:
=> value of firm = sum of value of individual assets
$=>$ change in value of firm from decision $=$ NPV of decision
Appendix to Chapter 3: The Price of Risk
A. Risky Verses Risk-Free Cash Flows

1. Key ideas
1) investors prefer less risk other things equal

Reason: for most people a $\$ 1$ loss is a bigger deal than a $\$ 1$ gain
2) Risk premium: extra return demanded by investors for holding risky assets instead of the risk-free asset (generally assumed to be U.S. Treasuries for investors in the U.S.)
=> compensates investors for taking any risk
2. Risk premium on the market
=> additional return can expect for taking the market's risk
Note: the market risk premium will increase if:

1) the risk of the market increases or,
2) if investors become more risk averse
3. Risk premium on a security

Key => Depends on two things:

1) risk premium on market index
2) degree to which security's return varies with market index.
=> more varies with market, higher the risk premium
Ex. Assume the following:

- risk-free interest rate $=2 \%$
- a strong or weak economy is equally likely
- price of the market ETF: $\$ 100$
- payoff on stock market ETF depends on the economy as follows:
weak economy $=\$ 75$
strong economy $=\$ 139$
- payoff on Orange Inc. depends on the economy as follows:
weak economy $=\$ 95$
strong economy $=\$ 159$
Q: What are the expected cash flow next year, the possible returns, the expected return, and the risk premium on the market?
$\Rightarrow>$ expected cash flow for the market index $=107=\frac{1}{2}(\mathbf{7 5})+\frac{1}{2}(\mathbf{1 3 9})$
$\Rightarrow$ return on the market depends on the economy as follows:
Strong: $39 \%=\frac{\mathbf{1 3 9 - 1 0 0}}{\mathbf{1 0 0}}$
Weak: $-25 \%=\frac{\mathbf{7 5 - 1 0 0}}{\mathbf{1 0 0}}$
$\Rightarrow>$ expected return on the market index: $7 \%=\frac{\mathbf{1 0 7 - 1 0 0}}{\mathbf{1 0 0}}=\frac{\mathbf{1}}{\mathbf{2}}(\mathbf{3 9} \%)+\frac{\mathbf{1}}{\mathbf{2}}(-\mathbf{2 5} \%)$
$\Rightarrow$ risk premium on the market index $=5 \%=7-2$
Q: What is the no-arbitrage price of Orange Inc.?


## Q: How does the payoff on Orange compare to the payoff on the market?

=> Orange always pays $\$ 20$ more than the market
Q: How create a portfolio that is equivalent to buying Orange?

|  | \$ in one year <br> $\underline{\text { Weak }}$ |  |
| :--- | ---: | ---: |
| $\underline{\text { Transaction }}$ | $\underline{\text { Strong }}$ |  |
| Buy Orange |  |  |
| Equivalent Portfolio: |  |  |
| Buy market index | +759.00 | +139.00 |
| Buy risk-free bond | $\underline{\mathbf{2 0 . 0 0}}$ | $+\underline{\mathbf{2 0 . 0 0}}$ |
| Total | +95.00 | +159.00 |

Cost to build portfolio that is equivalent to buying Orange:
$=>$ Cost of equivalent portfolio $=119.61=\mathbf{1 0 0}+\frac{\mathbf{2 0}}{\mathbf{1 . 0 2}}=\mathbf{1 0 0}+\mathbf{1 9 . 6 1}$
=> arbitrage unless the price of Orange equals 119.61
Q: What is arbitrage profit if the price of Orange is $\$ 125$ instead of $\$ 119.61$ ? How do you create this profit?

| \$ in one year |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Transaction | \$ today | Weak | Strong | Transaction |
| Short-sell Orange | +125.00 | - 95.00 | - 159.00 | Buy back Orange, return |
| Buy market index | -100.00 | +75.00 | +139.00 | Payoff on market |
| Buy risk-free bond | - $\underline{19.61}$ | + $\mathbf{2 0 . 0 0}$ | +20.00 | Payoff on bond |
| Total | +5.39 | 0.00 | 0.00 |  |

Q: What is the arbitrage profit if the price of Orange is $\$ 110$ instead of $\$ 119.61$ ?

|  | \$ in one year |  |  |  |
| :--- | ---: | ---: | ---: | :--- |
| Transaction | $\underline{\$ \text { today }}$ | $\underline{\text { Weak }}$ | $\underline{\text { Strong }}$ | Transaction |
| Buy Orange | $-\mathbf{1 1 0 . 0 0}$ | $\mathbf{+ 9 5 . 0 0}$ | $+\mathbf{+ 1 5 9 . 0 0}$ | Payoff Orange |
| Short-sell market index | $+\mathbf{1 0 0 . 0 0}$ | $-\mathbf{7 5 . 0 0}$ | $\mathbf{- 1 3 9 . 0 0}$ | Buy back market |
| Short-sell risk-free bond | $\underline{+\mathbf{1 9 . 6 1}}$ | $\mathbf{- \mathbf { 2 0 . 0 0 }}$ | $\mathbf{- \underline { \mathbf { 2 0 . 0 0 } }}$ | Buy back bond |
| Total | $\mathbf{+ 9 . 6 1}$ | $\mathbf{0 . 0 0}$ | $\mathbf{0 . 0 0}$ |  |

Q: What are the possible returns, expected return, and risk premium on Orange if it is correctly priced at $\$ 119.61$ ?

Return on Orange if strong economy $=\mathbf{3 2 . 9 \%}=\frac{\mathbf{1 5 9 - 1 1 9 . 6 1}}{\mathbf{1 1 9 . 6 1}}$
Return on Orange if weak economy $=\mathbf{- 2 0 . 6 \%}=\frac{\mathbf{9 5 - 1 1 9 . 6 1}}{\mathbf{1 1 9 . 6 1}}$
Note: return on Orange less volatile than the market ( $\mathbf{+ 3 9 \%}$ or $\mathbf{- 2 5 \%}$ )
Q: How should the risk premium on Orange compare to the market (5\%)?
=> should be less
Expected cash flow for Orange $=\frac{1}{2}(\mathbf{1 5 9})+\frac{\mathbf{1}}{\mathbf{2}}(\mathbf{9 5})=\mathbf{1 2 7}$
Expected return on Orange $=\frac{\mathbf{1 2 7}-\mathbf{1 1 9 . 6 1}}{119.61}=\frac{\mathbf{1}}{2}(\mathbf{3 2 . 9} \%)+\frac{1}{2}(-\mathbf{2 0 . 6} \%)=.062=$ 6.2\%

Risk premium on Orange $=.042=.062-.02$
Note: Risk premium less than $5 \%$ on market.
Ex. Assume that all of the information in the Orange example still holds (Market index trades for $\$ 100$ today and pays, $\$ 75$ or $\$ 139$ a year from today. Risk-free rate equals $2 \%$ ). Assume also that we can invest in Pineapple which pays $\$ 65$ when the economy is weak and $\$ 129$ when the economy is strong?

Q1: What is the no-arbitrage price for Pineapple?
Q2: What is the arbitrage profit if Pineapple's price is $\$ 95$ or $\$ 80$ ?
Q3: If Pineapple is correctly priced, what are the possible returns, expected return, and risk premium on the stock?

Note: Pineapple always pays $\mathbf{\$ 1 0}$ less than the market.
Equivalent portfolio:

|  | \$ in one year |  |
| :--- | ---: | ---: |
| Transaction | $\underline{\text { Weak }}$ | $\underline{\text { Strong }}$ |
| Buy market index | $+\mathbf{+ 5 5 . 0 0}$ | $+\mathbf{+ 1 3 9 . 0 0}$ |
| Short-sell risk-free bond | $-\mathbf{1 0 . 0 0}$ | $\underline{\mathbf{- 1 0 . 0 0}}$ |
| Total | $+\mathbf{+ 6 5 . 0 0}$ | $\mathbf{+ 1 2 9 . 0 0}$ |

Cost of equivalent portfolio $=\mathbf{9 0 . 2 0}=\mathbf{1 0 0}-\frac{\mathbf{1 0}}{\mathbf{1 . 0 2}}=\mathbf{1 0 0}-\mathbf{9 . 8 0}$
A1: no-arbitrage price of Pineapple $=\$ 90.20$
A2 (\$95): Arbitrage profit if the price of Pineapple is $\$ 95$ instead of the no-arbitrage price of $\$ 90.20$.


A2 (\$80): Arbitrage profit if the price of Pineapple is $\$ 80$ instead of the no-arbitrage price of $\$ 90.20$.

| Table 8 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | \$ in | year |  |
| Transaction ( $\mathrm{t}=0$ ) | \$ today | Weak | Strong | Transaction ( $\mathrm{t}=1$ ) |
| Buy Pineapple | -80.00 | +65.00 | +129.00 | Payoff Orange |
| Short-sell market index | +100.00 | - 75.00 | - 139.00 | Buy to cover market |
| Buy risk-free bond | -9.80 | +10.00 | +10.00 | Payoff on bond |
| Total | +10.20 | 0.00 | 0.00 |  |

A3: Possible returns, expected return, and risk premium on Pineapple if it is correctly priced at $\$ 90.20$

Return on Pineapple if strong economy $=43 \%=\frac{\mathbf{1 2 9 - 9 0 . 2 0}}{\mathbf{9 0 . 2 0}}$
Return on Pineapple if weak economy $=-27.9 \%=\frac{\mathbf{6 5 - 9 0 . 2 0}}{\mathbf{9 0 . 2 0}}$
Note: return on Pineapple is more volatile than the market ( $+39 \%$ or $-25 \%$ )
Expected return on Pineapple $=.0755=7.55 \%=\frac{1}{2}(\mathbf{4 3} \%)+\frac{1}{2}(-\mathbf{2 7 . 9} \%)$
Risk premium on Pineapple $=.0555=.0755-.02$
Note: Risk premium on Pineapple larger than 5\% on market.

## B. Arbitrage with Transaction Costs

Transaction costs: costs to trade securities
Note: transaction costs include:

1. commission to broker
2. bid-ask spread: difference between bid price and ask price
3. fees to borrow stock (varies with demand for shares to short)

Key: Transaction costs lead to the following modifications of earlier definitions:
Normal market $=>$ no arbitrage after transaction costs covered
Law of one price $=>$ difference in prices for equivalent securities must be less than transaction costs of engaging in arbitrage
No arbitrage price $=>$ differences between price and the $\operatorname{PV}(\mathrm{CF})$ must be less than transaction costs
Portfolio prices $=>$ Difference between the price of a portfolio and the sum of the prices of assets in the portfolio must be less than the transaction costs to build or break apart the portfolio

