

Note: Answer the following on a per-share basis.

Assume you want to value a call with a strike price of \$18 that expires two years from today. The price of the stock on which the put will be written is \$20, but the price will either rise 20% or fall by 10% each of the next two years. Assume that the risk-free interest rate equals 4% per year.

- What is the value today of the call?
- If you create a portfolio today that is equivalent to the call, what will be the makeup of the portfolio?
- Assume the stock price falls next year. What trades would you have to make a year from today to rebalance your portfolio?
if stock rises both years
- What trades will be required two years from today to close out your portfolio? What cash flows will occur?

a. $S_u = 20(1.2) = 24; S_d = 20(.9) = 18; S_{uu} = 24(1.2) = 28.8; S_{ud} = S_{du} = 24(.9) = 21.6; S_{dd} = 18(.9) = 16.2$
 $C_{uu} = 10.8; C_{ud} = C_{du} = 3.6; C_{dd} = 0$

$$\Delta_u = \frac{10.8 - 3.6}{28.8 - 21.6} = +1; B_u = \frac{3.6 - 1(21.6)}{1.04} = -17.3077; C_u = 24(1) - 17.3077 = 6.6923$$

$$\Delta_d = \frac{3.6 - 0}{21.6 - 16.2} = +0.667; B_d = \frac{0 - (.67)(16.2)}{1.04} = -10.3846; C_d = 18(.667) - 10.3846 = 1.6154$$

$$\Delta = \frac{6.6923 - 1.6154}{24 - 18} = .84615; B = \frac{1.6154 - .84615(18)}{1.04} = -13.0917;$$

$$C = 20(.84615) - 13.0917 = 3.8314$$

b. Buy 0.84615 shares + short sell 13.0917 bonds

c. Sell .1795 shares (.84615 - .66667); Buy to cover 3.2308 bonds (-10.3846 - (-13.0917)(1.04))

d. Sell 1 share @ 28.8; Buy to cover 1/8 of bonds (17.3077)(1.04)